## EXAM 1

Math 212, 2014 Summer Term 1, Clark Bray.
You have 75 minutes.
No notes, no books, no calculators.
YOU MUST SHOW ALL WORK AND EXPLAIN ALL REASONING TO RECEIVE CREDIT. CLARITY WILL BE CONSIDERED IN GRADING.

All answers must be simplified. All of the policies and guidelines on the class webpages are in effect on this exam.

Good luck!

Name $\qquad$

1. $\qquad$
"I have adhered to the Duke Community
Standard in completing this examination."
2. $\qquad$
Signature: $\qquad$
3. $\qquad$
4. $\qquad$
5. $\qquad$
6. $\qquad$
7. $\qquad$
Total Score $\qquad$ (/100 points)
8. $\qquad$
9. (12 pts) Let $\vec{v}=(3,5,1)$ and $\vec{w}=(2,1,1)$.
(a) Compute $\vec{v} \cdot \vec{w}$ and $\operatorname{comp}_{\vec{w}}(\vec{v})$.
(b) Find the unit vector that points in the direction of the vector $\vec{w}$.
(c) The vector $\vec{a}$ is parallel to $\vec{w}$, the vector $\vec{b}$ is orthogonal to $\vec{w}$, and $\vec{a}+\vec{b}=\vec{v}$. Find $\vec{a}$ and $\vec{b}$. (Hint: The previous parts of this question should be useful.)
10. (10 pts) Show, as in class, that if $\vec{v} \times \vec{w} \neq \overrightarrow{0}$, then the list $\vec{v}, \vec{w}, \vec{v} \times \vec{w}$ is in right hand order.
11. (10 pts) The plane $P$ has equation $2 x-3 y+5 z=3$; and $\vec{v}=(1,2,3)$. Find a parametrization of the line that is parallel to $P$, perpendicular to $\vec{v}$, and passes through the point $\vec{a}=(3,4,5)$.
12. (10 pts) Find the equation in spherical coordinates for the sphere of radius 13 centered at the point $(x, y, z)=(3,4,12)$.
13. (12 pts) The surface $S$ is the part of the cone $z=1-r$ that is above the $x y$-plane. Find a parametrization, giving $x, y$, and $z$ as functions of two other parameters.
14. (12 pts) In this question we consider the solution set of $-x^{2}-y^{2}+z^{2}=1$.
(a) Around what line is the solution set rotationally symmetric?
(b) Draw the cross section of this surface in a corresponding half plane.
(c) Find a function $f$ whose graph is the lower part of this surface. (Indicate clearly the domain and target for this function.)
15. (12 pts) Find a function $g$ for which one of the level sets is the sphere of radius 4 centered at the point ( $1,2,3$ ). (Indicate clearly the domain and target for this function.)
16. (12 pts) The vectors $\vec{v}_{i}$ of the left matrix in the product below are all orthogonal to each other, and have magnitudes 2,3 , and 5 , respectively. Compute $\vec{a}_{1} \cdot \vec{v}_{3}$.

$$
\left(\begin{array}{ccc}
\mid & \mid & \mid \\
\vec{v}_{1} & \vec{v}_{2} & \vec{v}_{3} \\
\mid & \mid & \mid
\end{array}\right)\left(\begin{array}{ccc}
1 & 3 & 2 \\
2 & 1 & 4 \\
8 & 7 & 9
\end{array}\right)=\left(\begin{array}{ccc}
\mid & \mid & \mid \\
\vec{a}_{1} & \vec{a}_{2} & \vec{a}_{3} \\
\mid & \mid & \mid
\end{array}\right)
$$

9. (10 pts) A car starts at the location $(3,5)$, and moves with velocity given by $(4 \sin (2 t), 6 t \sin (t))$. Compute the location of the car at $t=\pi / 4$.
