EXAM 2

Math 212, 2015 Summer Term 1, Clark Bray.

You have 75 minutes.

No notes, no books, no calculators.

YOU MUST SHOW ALL WORK AND EXPLAIN ALL REASONING TO RECEIVE CREDIT. CLARITY WILL BE CONSIDERED IN GRADING. All answers must be simplified. All of the policies and guidelines on the class webpages are in effect on this exam.

Good luck!

	Name		
1		"I have adhered to the Du Standard in comple	ting this
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7		Total Score	(/100 points)

- 1. (15 pts) In this question we consider the function defined by $f(x,y) = x^2 e^y \sin(\pi xy)$.
 - (a) Compute the directional derivatives below, by any means from this course.

$$D_{\vec{e}_1}f(x,y)$$
 and $D_{\vec{e}_2}f(x,y)$

(b) Is f differentiable? Explain your reasoning fully.

(c) Use parts (a) and (b) above (and note specifically where you use them!) to compute the directional derivative $D_{\vec{v}}f(\vec{a})$, where $\vec{v} = (4, 2)$ and $\vec{a} = (1, 0)$.

2. (10 pts) The variables w and z are functions of x and y, and x and y are the usual polar functions of r and θ (with r > 0). Simplify the expression below.

$$\frac{\partial}{\partial \theta} \Big(x \, w_x \Big)$$

3. (10 pts) We have f(u, v) = (x, y), g(x, y) = (s, t), and h(s, t) = (p, q). We also know that, for certain values of u and v (and the resulting values of the other variables),

$$J_f = \begin{pmatrix} 1 & 6 \\ 3 & 4 \end{pmatrix}$$
 and $J_g = \begin{pmatrix} 2 & 5 \\ 1 & 3 \end{pmatrix}$

Write an expression for $\frac{\partial q}{\partial v}$ in terms of the partial derivatives of the function h.

4. (15 pts) Use the definition of directional derivative (do NOT use partial derivatives or the gradient vector or equivalent) to find the slope of the tangent line to the graph of $f(x, y) = x^2 y$ at the point with x = 1, y = 2, in the direction indicated by the vector $\vec{v} = (3, 4)$.

5. (15 pts) Use the gradient vector to find the equation of the tangent plane to the graph in the previous question at the indicated point.

6. (15 pts) The solid R is bounded by the surfaces x + y = 2, x - y = 2, x = 0, z = 0, and $z = 4 + x^2$. Set up, but do not evaluate, a (single) triple iterated integral representing $\iiint_R f(x, y, z) dV$ 7. (20 pts) The parallelogram P in \mathbb{R}^2 has edge vectors (3, 5) and (-1, 4). Set up, but do not evaluate, a (single) double iterated integral to compute $\iint_P x \, dx \, dy$. (Hint: Use a linear transformation L, with $L(\vec{e_1}) = (3, 5)$ and $L(\vec{e_2}) = (-1, 4)$, to relate P to the unit square.)