EXAM 1

Math 212, 2018-2019 Summer Term 1 (Marine Lab), Clark Bray.

You have 75 minutes.

No notes, no books, no calculators.

YOU MUST SHOW ALL WORK AND EXPLAIN ALL REASONING TO RECEIVE CREDIT. CLARITY WILL BE CONSIDERED IN GRADING. All answers must be simplified. All of the policies and guidelines on the class webpages are in effect on this exam.

Good luck!

Na	ame
1	"I have adhered to the Duke Community Standard in completing this examination."
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	Total Score $(/100 \text{ points})$

- 1. (15 pts) The line L_1 has symmetric equations 2x 4 = 3y 3 = z 3, and the line L_2 is parametrized by (x, y, z) = (1 + t, 4 3t, -1 + 4t).
 - (a) Do these lines intersect? If yes, find the point of intersection.

(b) Find the equation of the plane parallel to L_1 that contains L_2 .

2. (5 pts) The plane P has normal vector (1, 2, 3) and contains the point (2, 1, 1). Find the distance from P to (0, 4, 5). (Hint: This distance is a component.)

3. (10 pts) Describe a geometric process by which you could generate the surface with equation $z = \ln(x^2 + y^2)$ from a standard curve of high school algebra.

- 4. (10 pts) Find the equation of the surface that results from applying to the unit sphere the following sequence of transformations.
 - (a) Stretch by a factor of 2 in the x direction;
 - (b) Shift by a distance 4 in the positive x direction;
 - (c) Shift by a distance 3 in the positive y direction;
 - (d) Reflect through the xz-plane.

- 5. (30 pts) The surface S has equation $x^2z + z x^3y = x^4y^3$.
 - (a) Is S a level set of any function f? If so, find such a function, its domain, and its target.

(b) Is S the graph of any function g? If so, find such a function, its domain, and its target.

(c) Is S the image of any function h? If so, find such a function, its domain, and its target.

6. $(15 \ pts)$ Evaluate the following limit or show that it does not exist.

$$\lim_{(x,y)\to(0,0)}\frac{x^4}{(x^2+y^2)^2}$$

- 7. (15 pts) The linear transformation $L : \mathbb{R}^2 \to \mathbb{R}^2$ acts on vectors $\vec{v} \in \mathbb{R}^2$ by first rotating counterclockwise around the origin by $\pi/6$, then reflecting over the *y*-axis.
 - (a) Find the matrix M that represents L.

(b) Use an operation of matrix algebra to find the matrix that represents $L \circ L$.